

R dalam Analisis korelasi dan Regresi linier sederhana

BAB 2

Input Data - Cara I

IQ	IPK
99	3.00
118	3.50
108	3.20
110	3.25
97	2.70
120	3.50
105	3.25

- `IQ <- c(99, 118, 108, 110, 97, 120, 105)`
- `IPK <-c(3, 3.5, 3.2, 3.25, 2.7, 3.5, 3.25)`

Input Data - Cara I

IQ	IPK
99	3.00
118	3.50
108	3.20
110	3.25
97	2.70
120	3.50
105	3.25

- `IQ <- scan()`
1 : 99 118 108 110 97 120 105
8: (*enter*)
- `IPK <-scan()`
1: 3 3.5 3.2 3.25 2.7 3.5 3.25

Example

```
> IQ<-scan()  
1: 99  
2: 118  
3: 108  
4: 110  
5: 97  
6: 120  
7: 105  
8:  
Read 7 items  
> IPK<-scan()  
1: 3  
2: 3.5  
3: 3.2  
4: 3.25  
5: 2.7  
6: 3.5  
7: 3.25  
8:  
Read 7 items
```

Analisis Korelasi

- ▶ Mengetahui nilai korelasi
- ▶ Melakukan uji korelasi

IQ	IPK
99	3.00
118	3.50
108	3.20
110	3.25
97	2.70
120	3.50
105	3.25

Menggunakan command

```
> cor(IPK,IQ)
```

```
> cor.test(IPK,IQ)
```

Output

1. Nilai korelasi

```
> cor(IPK, IQ)
[1] 0.9381326
> cor.test(IPK, IQ)
```

Pearson's product-moment correlation

```
data: IPK and IQ
t = 6.058, df = 5, p-value = 0.001768
alternative hypothesis: true correlation is not equal to 0
95 percent confidence interval:
 0.6305094 0.9910472
sample estimates:
      cor
0.9381326
```

- ▶ Nilai Korelasi antara IPK, IQ adalah 0.9381326
- ▶ Kesimpulan Uji Hipotesis Nilai Korelasi tidak sama dengan 0

2. Melakukan uji korelasi

```
> cor(IPK, IQ)
[1] 0.9381326
> cor.test(IPK, IQ)
```

```
Pearson's product-moment correlation
```

```
data: IPK and IQ
t = 6.058, df = 5, p-value = 0.001768
alternative hypothesis: true correlation is not equal to 0
95 percent confidence interval:
 0.6305094 0.9910472
sample estimates:
      cor
0.9381326
```

i. Menyusun hipotesis

H0 : Tidak ada korelasi antara IPK dan IQ ($\text{cor}(\text{IPK}, \text{IQ}) = 0$)

H1 : Terdapat korelasi antara IPK dan IQ ($\text{cor}(\text{IPK}, \text{IQ}) \neq 0$)

```
> cor(IPK, IQ)
[1] 0.9381326
> cor.test(IPK, IQ)
```

Pearson's product-moment correlation

```
data: IPK and IQ
t = 6.058, df = 5, p-value = 0.001768
alternative hypothesis: true correlation is not equal to 0
95 percent confidence interval:
 0.6305094 0.9910472
sample estimates:
      cor
0.9381326
```

ii. Pilih tingkat signifikansi $\alpha=5\%=0.05$

iii. Daerah Kritis (daerah penolakan hipotesis null)

- ▶ P-value < $\alpha = 0.05$
- ▶ Karena $\alpha = 0.05 > p\text{-value}=0.001768$ maka H_0 ditolak
- ▶ D.k.l ada korelasi antara IPK dan IQ

Analisis Regresi

- ▶ Membuat persamaan
- ▶ Mengetahui hasil regresi
- ▶ Mengetahui uji anova

```
> fm <- lm(IPK ~ IQ)  
> summary(fm)  
> anova(fm)
```

Persamaannya?

$$\text{IPK} = -0.064150 + 0.030184 \cdot \text{IQ}$$

```
> fm<-lm(IPK~IQ)
> summary(fm)
```

```
Call:
lm(formula = IPK ~ IQ)
```

```
Residuals:
```

```
      1      2      3      4      5      6      7
0.075965 0.002475 0.004312 -0.006055 -0.163667 -0.057892 0.144863
```

```
Coefficients:
```

```
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.064150   0.540328  -0.119  0.91012
IQ           0.030184   0.004982   6.058  0.00177 **
```

```
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 0.1067 on 5 degrees of freedom
Multiple R-squared:  0.8801,    Adjusted R-squared:  0.8561
F-statistic: 36.7 on 1 and 5 DF,  p-value: 0.001768
```

Uji Hipotesisnya

```
> anova(fm)
```

```
Analysis of Variance Table
```

```
Response: IPK
```

```
      Df Sum Sq Mean Sq F value    Pr(>F)
IQ      1  0.41804  0.41804  36.699 0.001768 **
Residuals 5  0.05696  0.01139
```

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- ▶ Hipotesis

- ▶ H-null : $B = 0$

- ▶ H-alt : $B \neq 0$

- ▶ Daerah Kritis: $p < 0.05$

- ▶ Statistik uji: $F = 36.699$; $p=0.001768$

- ▶ Hasil uji

- $p = 0.001768 < \alpha = 0.05$

- ▶ Kesimpulan

- Hipotesis null tidak diterima, dkl. IQ mempunyai pengaruh terhadap IPK

Regresi pada R

```
> fm<-lm(IPK~IQ)
> summary(fm)
```

Call:

```
lm(formula = IPK ~ IQ)
```

Residuals:

```
      1      2      3      4      5      6      7
0.075965 0.002475 0.004312 -0.006055 -0.163667 -0.057892 0.144863
```

Coefficients:

```
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.064150   0.540328  -0.119  0.91012
IQ           0.030184   0.004982   6.058  0.00177 **
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.1067 on 5 degrees of freedom

Multiple R-squared: 0.8801, Adjusted R-squared: 0.8561

F-statistic: 36.7 on 1 and 5 DF, p-value: 0.001768

Uji ANOVA

```
> anova(fm)
```

```
Analysis of Variance Table
```

```
Response: IPK
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
IQ	1	0.41804	0.41804	36.699	0.001768 **
Residuals	5	0.05696	0.01139		

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Uji kenormalan

- ▶ Dengan menggunakan uji shapiro wilk

```
> shapiro.test(residuals(fm))
```

```
Shapiro-Wilk normality test
```

```
data: residuals(fm)  
W = 0.96361, p-value = 0.8491
```

- ▶ i. Menyusun hipotesis
 - ▶ H0: residual berdistribusi normal
 - ▶ H1: residual tidak berdistribusi normal
- ii. Pilih tingkat signifikansi $\alpha=0.05$
- iii. Statistika Uji Shapiro Wilk
 - W=0.96361
 - p-value=0.8491
 - Karena $\alpha=0.05 < p\text{-value}=0.8491$ maka H0 tidak ditolak
 - D.k.l asumsi kenormalan dapat dipenuhi

Mencari residual

- ▶ Menghitung residual terstandar dengan fungsi `rstandard`

```
> sres<-rstandard(fm)
> sres[1:5]
      1          2          3          4          5
0.86633904 0.02886657 0.04363896 -0.06155248 -2.00228192
> sres[1:7]
      1          2          3          4          5          6
0.86633904 0.02886657 0.04363896 -0.06155248 -2.00228192 -0.73090337
      7
1.48480525
```

- ▶ Mencari observasi yang diduga outlier (studentized residual)

```
> sres[which(abs(sres)>2)]
      5
-2.002282
```